

Trigonometric Identities:

Reciprocal Identities

$$\cot(\theta) = \frac{1}{\tan(\theta)} \quad \sec(\theta) = \frac{1}{\cos(\theta)} \quad \csc(\theta) = \frac{1}{\sin(\theta)}$$

Quotient Identities

$$\tan(\theta) = \frac{\sin(\theta)}{\cos(\theta)} \quad \cot(\theta) = \frac{\cos(\theta)}{\sin(\theta)}$$

Pythagorean Identities

$$\sin^2(\theta) + \cos^2(\theta) = 1 \quad \tan^2(\theta) + 1 = \sec^2(\theta) \quad 1 + \cot^2(\theta) = \csc^2(\theta)$$

Even-Odd Identities

$$\begin{aligned} \sin(-\theta) &= -\sin(\theta) & \cos(-\theta) &= \cos(\theta) & \tan(-\theta) &= -\tan(\theta) \\ \csc(-\theta) &= -\csc(\theta) & \sec(-\theta) &= \sec(\theta) & \cot(-\theta) &= -\cot(\theta) \end{aligned}$$

Cofunction Identities

$$\begin{aligned} \cos(\theta) &= \sin\left(\frac{\pi}{2} - \theta\right) & \cot(\theta) &= \tan\left(\frac{\pi}{2} - \theta\right) & \csc(\theta) &= \sec\left(\frac{\pi}{2} - \theta\right) \\ \sin(\theta) &= \cos\left(\frac{\pi}{2} - \theta\right) & \tan(\theta) &= \cot\left(\frac{\pi}{2} - \theta\right) & \sec(\theta) &= \csc\left(\frac{\pi}{2} - \theta\right) \end{aligned}$$

Sum and Difference Identities

$$\begin{aligned} \cos(A+B) &= \cos(A)\cos(B) - \sin(A)\sin(B) & \cos(A-B) &= \cos(A)\cos(B) + \sin(A)\sin(B) \\ \sin(A+B) &= \sin(A)\cos(B) + \cos(A)\sin(B) & \sin(A-B) &= \sin(A)\cos(B) - \cos(A)\sin(B) \\ \tan(A+B) &= \frac{\tan(A) + \tan(B)}{1 - \tan(A)\tan(B)} & \tan(A-B) &= \frac{\tan(A) - \tan(B)}{1 + \tan(A)\tan(B)} \end{aligned}$$

Double-angle Formulas

$$\begin{aligned} \cos(2A) &= \cos^2(A) - \sin^2(A) & \cos(2A) &= 1 - 2\sin^2(A) & \cos(2A) &= 2\cos^2(A) - 1 \\ \sin(2A) &= 2\sin(A)\cos(A) & \tan(2A) &= \frac{2\tan(A)}{1 - \tan^2(A)} \end{aligned}$$

Product-to-Sum Identities

$$\cos(A) \cos(B) = \frac{1}{2} [\cos(A + B) + \cos(A - B)]$$

$$\sin(A) \sin(B) = \frac{1}{2} [\cos(A - B) - \cos(A + B)]$$

$$\sin(A) \cos(B) = \frac{1}{2} [\sin(A + B) + \sin(A - B)]$$

$$\cos(A) \sin(B) = \frac{1}{2} [\sin(A + B) - \sin(A - B)]$$

Sum-to-Product Identities

$$\sin(A) + \sin(B) = 2 \sin\left(\frac{A + B}{2}\right) \cos\left(\frac{A - B}{2}\right)$$

$$\sin(A) - \sin(B) = 2 \cos\left(\frac{A + B}{2}\right) \sin\left(\frac{A - B}{2}\right)$$

$$\cos(A) + \cos(B) = 2 \cos\left(\frac{A + B}{2}\right) \cos\left(\frac{A - B}{2}\right)$$

$$\cos(A) - \cos(B) = -2 \sin\left(\frac{A + B}{2}\right) \sin\left(\frac{A - B}{2}\right)$$

Half-Angle Identities

$$\cos\left(\frac{A}{2}\right) = \pm \sqrt{\frac{1 + \cos(A)}{2}} \quad \cos^2(A) = \frac{1 + \cos(2A)}{2}$$

$$\sin\left(\frac{A}{2}\right) = \pm \sqrt{\frac{1 - \cos(A)}{2}} \quad \sin^2(A) = \frac{1 - \cos(2A)}{2}$$

$$\tan\left(\frac{A}{2}\right) = \pm \sqrt{\frac{1 - \cos(A)}{1 + \cos(A)}} \quad \tan\left(\frac{A}{2}\right) = \frac{\sin(A)}{1 + \cos(A)} \quad \tan\left(\frac{A}{2}\right) = \frac{1 - \cos(A)}{\sin(A)}$$